

1 **Polar amplification in idealized climates: the role of ice,**  
2 **moisture, and seasons**

3 **Nicole Feldl<sup>1</sup>, Timothy M. Merlis<sup>2</sup>**

4 <sup>1</sup>Department of Earth and Planetary Sciences, University of California, Santa Cruz, California, USA

5 <sup>2</sup>Department of Atmospheric and Oceanic Sciences, McGill University, Montreal, Quebec, Canada

6 **Key Points:**

- 7 • Annual-mean polar amplification is insensitive to the inclusion of a seasonal cy-  
8 cle of insolation with a simple ice-albedo feedback.
- 9 • Fidelity of the seasonality of polar warming occurs under the combined influence  
10 of seasons and thermodynamic-ice processes.
- 11 • The ice-albedo feedback and moist energy transport make comparable and nearly  
12 additive contributions to polar-amplified warming.

## Abstract

Polar amplification is simulated across models of various complexities, yet uncertainty in attribution remains due to interactions among local feedbacks and poleward energy transports. Here, the role of sea-ice processes, moist energy transport, and the seasonal cycle of insolation are systematically investigated in two models, an energy balance model and an idealized general circulation model. Compared to a simple ice-albedo feedback, seasonal polar warming and transport changes are profoundly affected by the combined influence of seasons and thermodynamic-ice processes. A summer warming minimum occurs where temperatures are in their melting regime, and a maximum occurs where thick, cold ice preconditions a large radiatively forced response. Despite this enhanced winter warming, the annual-mean polar amplification is modestly reduced. When latent heat transport is disabled, polar amplification is further reduced by a factor of 1.7 across the range of ice representations, suggestive of a superposition of warming by ice and moist processes.

## Plain Language Summary

Since the 1970s, simulations of climate change have predicted warming that is greatest in polar regions. This polar-amplified warming is ubiquitous, though uncertain in magnitude, in climate models subjected to increases in greenhouse gases and has been variously attributed to the ice-albedo feedback, associated with the retreat of reflective sea ice; the lapse rate feedback, associated with the uneven warming of the Arctic atmosphere; and changes in heat transport by atmospheric circulations. In this study, we turn to highly simplified climate models to isolate the role of sea ice, moisture, and seasons on polar amplification and to explore their interactions. We find that, in order to reproduce the seasonality of polar warming in a manner consistent with both observations and state-of-the-art climate models, it is necessary to model the changing thickness of sea ice and not just its retreat. This effect works in concert with moisture transport by the atmosphere to further enhance polar amplification. Together, the findings imply that sea-ice loss leads to winter warming that would promote a lapse rate feedback and that the increase in moist energy transport would also lead, in more complex models, to additional warming by increasing the water-vapor greenhouse effect.

## 1 Introduction

Polar amplification has been a robust projection since the earliest climate simulations; nevertheless, the magnitude and timing of the surface warming at high latitudes remains poorly constrained. The phenomenon has been variously attributed to the ice-albedo feedback (e.g., Manabe & Wetherald, 1975), to an increase in poleward atmosphere-ocean energy transport (e.g., Holland & Bitz, 2003; Hwang et al., 2011), and to temperature feedbacks (e.g., Winton, 2006; Pithan & Mauritsen, 2014); recent work has highlighted the interconnected nature of the summertime and wintertime feedbacks over sea-ice regions (Boeke & Taylor, 2018; Dai et al., 2019; Feldl et al., 2020). Hence the uncertainty in projections of climate change, commonly expressed as intermodel spread, arises in part from incomplete understanding of the interaction among these processes. While simple models tend to emphasize that poleward energy transport *can* produce polar-amplified warming purely through moist atmospheric processes (e.g., Roe et al., 2015; Merlis & Henry, 2018), they often neglect critical real-world physics such as ice thermodynamics and seasonal variations in insolation. Investigation of a current gap in the modeling hierarchy—that of the idealized moist, icy, and seasonal climate model—reveals how energy transport and sea-ice processes work in concert to produce latitudinally and seasonally varying warming.

For our idealized climate models, we consider both energy balance models (EBMs) and general circulation models (GCMs). Traditional EBMs represent atmospheric en-

63 energy transport as a diffusive process proportional to the meridional gradient of temper-  
64 ature and include the ice-albedo feedback via a temperature-dependent surface albedo  
65 (Budyko, 1969; Sellers, 1969; North, 1975; North et al., 1981). As a consequence of these  
66 parametrizations, when subject to a uniform radiative forcing, the simulated warming  
67 is greatest at polar latitudes. When the ice albedo is locked (Merlis, 2014) or the surface-  
68 albedo feedback disabled (Armour et al., 2019), warming is uniform, and every latitude  
69 warms by the reference climate sensitivity. Thus polar amplification in the dry EBM re-  
70 quires spatial heterogeneity in radiative feedbacks or radiative forcing in order to drive  
71 changes in atmospheric energy transport. The results of the early modeling studies in  
72 particular have contributed to the prevailing view that polar amplification requires the  
73 presence of sea-ice processes.

74 The rise of the moist EBM in recent years has challenged the necessity of polar feed-  
75 backs in producing polar-amplified warming. In the moist EBM, moist static energy re-  
76 places temperature in the calculation of diffusive energy transport, which allows for an  
77 increase in the latent component of energy transport with warming (Flannery, 1984). Ac-  
78 counting for the effects of latent heat on energy transport improves the ability of EBMs  
79 to mimic the zonal-mean behavior of GCMs. Further, in contrast to their dry counter-  
80 parts, moist EBMs produce polar amplification even in the absence of spatially varying  
81 radiative forcing or feedbacks (Roe et al., 2015). This behavior can be understood as a  
82 result of the preferential increase in tropical water vapor with warming that, combined  
83 with down-gradient moist static energy diffusion, produces an increase in atmospheric  
84 energy transport. Moist EBMs can be coupled to a sea-ice parametrization (e.g., Lut-  
85 sko et al., 2020), prescribed with surface albedo changes (e.g., Hwang & Frierson, 2010),  
86 or neither (e.g., Merlis & Henry, 2018). Not surprisingly, when the ice-albedo feedback  
87 is enabled in one form or another, polar amplification is enhanced. We also note that  
88 two varieties of the moist EBM implementation are in common usage: a climatological  
89 version that integrates the governing equation numerically and does not prescribe pat-  
90 terns of feedbacks (Frierson et al., 2007; Merlis & Henry, 2018) and a perturbation ver-  
91 sion cast in terms of meridional patterns of radiative forcing, radiative feedbacks, ocean  
92 heat uptake, and anomalous moist static energy (Rose et al., 2014; Roe et al., 2015; Bo-  
93 nan et al., 2018; Armour et al., 2019). In this study we build upon the former so that  
94 sea ice is an interactive component of the climate system, allowing it to shape the con-  
95 trol climate and the response to warming.

96 Like moist EBMs, idealized GCMs are capable of producing polar amplification in  
97 the absence of sea-ice processes (Alexeev et al., 2005; Langen et al., 2012; Russotto &  
98 Biasutti, 2020), though the result is not ubiquitous and is likely model dependent (Feldl  
99 et al., 2017). For instance, Kim et al. (2018) showed that an aquaplanet simulation with  
100 clouds, seasonally varying insolation, and no ice-albedo feedback results in a notable lack  
101 of polar amplification, due to cancellation by polar cloud feedbacks, whereas under per-  
102 petual equinox conditions the otherwise identical model exhibits a strongly polar-amplified  
103 response due to increased atmospheric stability in polar regions. A number of questions  
104 arise regarding the fundamental role of seasonality in polar amplification that, given the  
105 disparity of previous results, warrant systematic investigation: Does the seasonal cycle  
106 of insolation affect annual-mean polar amplification in highly idealized models? What  
107 accounts for the seasonality of polar amplification itself? Further, given that sea-ice ther-  
108 modynamic processes are known to stabilize the climate (e.g., Bitz & Roe, 2004; Eisen-  
109 man & Wettlaufer, 2009), how important are thermodynamic processes associated with  
110 the seasonal cycle of sea-ice thickness in simulating polar amplification?

111 Evidence from models of various complexities suggest that local climate feedbacks  
112 work in concert with moist atmospheric processes to consistently produce polar-amplified  
113 warming. In what follows, we investigate the sensitivity of the warming pattern to the  
114 seasonal cycle and to sea-ice physics. We advance prior studies of annual-mean polar am-  
115 plification by incorporating the seasonal dynamics of sea ice in our EBM and idealized

116 GCM, following the work of Wagner and Eisenman (2015) on sea-ice instability, such that  
 117 we may consider both ice-thickness and ice-albedo effects. Of particular interest is the  
 118 potential for additivity of the different mechanisms contributing to polar amplification.  
 119 In other words, we seek to determine how the magnitude of polar amplification is controlled  
 120 by ice and moist-transport processes both combined and in isolation.

## 121 2 Methods

### 122 2.1 Moist EBM

The EBM used in this study, at its most comprehensive level, includes seasonal variations in climate, an idealized representation of sea-ice thickness and albedo, and an idealized representation of atmospheric energy transport as a moist diffusive process. The model evolves surface enthalpy,  $E(x, t)$  where  $x$  is sine of latitude, which represents the energy stored in the ocean mixed layer as sensible heat when the ocean is ice free or in sea ice as latent heat when the ocean is ice covered. For ice-free conditions, the governing equation is

$$c_w \frac{\partial T}{\partial t} = aS - (A + BT) - \nabla \cdot F_a + \mathcal{F} \quad (1)$$

123 with mixed-layer heat capacity  $c_w$ , surface temperature  $T$ , net solar radiation  $aS$ , out-  
 124 going longwave radiation (OLR)  $A + BT$ , divergence of atmospheric energy transport  
 125  $\nabla \cdot F_a$ , and uniform radiative forcing  $\mathcal{F}$ . Net solar radiation follows Wagner and Eisen-  
 126 man (2015), where insolation  $S(x, t) = S_0 - S_1 x \cos \omega t - S_2 x^2$ . The fraction of insolation  
 127 that is absorbed,  $a$ , depends on solar zenith angle, cloudiness, and surface albedo,  
 128 which we approximate as  $a_0 - a_2 x^2$  where  $E \geq 0$  (open-water conditions) and  $a_i$  where  
 129  $E < 0$  (ice). We use the following parameter values:  $c_w = 7.8 \text{ W yr m}^{-2} \text{ K}^{-1}$  (i.e.,  
 130 equivalent to a mixed-layer depth of 60 m),  $A = 195 \text{ W m}^{-2}$ ,  $B = 1.8 \text{ W m}^{-2}$ ,  $S_0 =$   
 131  $420 \text{ W m}^{-2}$ ,  $S_1 = 290 \text{ W m}^{-2}$ , and  $S_2 = 240 \text{ W m}^{-2}$ ,  $a_0 = 0.7$ ,  $a_2 = 0.1$ , and  $a_i =$   
 132  $0.4$ . In the control simulation,  $\mathcal{F} = 0 \text{ W m}^{-2}$ , and it is increased to  $\mathcal{F} = 8 \text{ W m}^{-2}$  in  
 133 the perturbation simulation. The magnitude of the forcing, roughly comparable to a  $4 \times$   
 134  $\text{CO}_2$  scenario, is sufficient to for the climate to become ice-free, though the results are  
 135 qualitatively similar for a smaller amplitude forcing that retains winter ice.

Divergence of atmospheric energy transport is assumed to be proportional to the meridional gradient of near-surface moist static energy (MSE)  $h$ :

$$\nabla \cdot F_a(x) = -\frac{\partial}{\partial x} D(1 - x^2) \frac{\partial h}{\partial x}, \quad (2)$$

with constant diffusivity  $D = 0.3 \text{ W m}^{-2} \text{ K}^{-1}$ . Building on the work of Wagner and Eisenman (2015), diffusion occurs in a ghost layer with heat capacity  $c_g = 0.098 \text{ W yr m}^{-2} \text{ K}^{-1}$ ; the ghost-layer temperature  $T_g$  is relaxed to the surface temperature with time scale  $\tau_g = 1 \times 10^{-5} \text{ yr}$  and evolves according to

$$c_g \frac{\partial T_g}{\partial t} = \frac{c_g}{\tau_g} (T - T_g) + D \nabla^2 h. \quad (3)$$

136 MSE is defined in units of temperature as  $h = T_g + c_p^{-1} L_v \mathcal{H} q_s(T_g)$  for latent heat of  
 137 vaporization  $L_v = 2.5 \times 10^6 \text{ J kg}^{-1}$ , relative humidity  $\mathcal{H} = 0.8$ , heat capacity of air at  
 138 constant pressure  $c_p = 1004.6 \text{ J kg}^{-1} \text{ K}^{-1}$ , and saturation vapor pressure  $q_s$ . Numerically,  
 139 this approach enables us to perform a semi-implicit time-stepping method on  $T_g$ ,  
 140 in contrast to the forward Euler method performed on  $T$ , though we note saturation specific  
 141 humidity is calculated on the previous time step for convenience. Alternatively, MSE  
 142 can be linearized about a spatially varying climatological temperature (e.g., Merlis & Henry,  
 143 2018) to have a more thoroughly semi-implicit time discretization, which produces indistinguishable  
 144 results.

Sea-ice thickness,  $h_i$  is governed by the balance between the vertical heat flux upward through the ice and the surface energy flux

$$\frac{k(T_m - T_0)}{h_i} = -aS + A + B(T_0 - T_m) + \nabla \cdot F_a - \mathcal{F}, \quad (4)$$

145 with ice thermal conductivity  $k = 2 \text{ W m}^{-1} \text{ K}^{-1}$  and melting point  $T_m = 0^\circ\text{C}$  (Wagner  
146 & Eisenman, 2015). From Equation 4, we obtain the freezing temperature of ice,  $T_0$ , used  
147 to determine the ice regime. In the freezing regime,  $T_0 < T_m$  and  $E < 0$ ; the energy  
148 flux is balanced by subfreezing surface temperature, and  $T = T_0$ . In the melting regime,  
149  $T_0 \geq T_m$  and  $E < 0$ , and surface temperature remains at the melting point,  $T = T_m$ .  
150 Open-water conditions are included by adding a third surface temperature regime: if  $E \geq$   
151  $0$ ,  $T = E/c_w$ , and (1) governs the surface's evolution.

152 The model is integrated numerically over the domain  $-1 < x < 1$  with 120 grid  
153 points spaced uniformly in  $x$  and 1000 time steps per year.

## 154 2.2 GCM

155 The idealized moist GCM builds on the work of Frierson et al. (2006) and includes  
156 a gray-radiation atmosphere and an idealized hydrological cycle. Water vapor is advected  
157 by the resolved-scale flow, undergoing condensation when supersaturated, and is sub-  
158 ject to a simple moist convection parameterization for unresolved convection (Frierson  
159 et al., 2007). Insolation varies seasonally according to a circular orbit with Earth's obliquity  
160 ( $23.45^\circ$ ) and a 360-day year. A top-of-atmosphere coalbedo that is a time-independent  
161 function of latitude  $\phi$  is given by  $a^{TOA} = a_0^{TOA} + \Delta a^{TOA}(3 \sin^2 \phi - 1)/2$ , which repre-  
162 sents the atmosphere's contribution, primarily clouds, to the planetary albedo. We use  
163  $a_0^{TOA} = 0.68$  and  $\Delta a^{TOA} = -0.2$ , following North et al. (1981). An additional, temperature-  
164 dependent surface albedo is applied with a value of 0.4 for sub-freezing temperatures and  
165 0.1 otherwise. The surface boundary condition follows the formulation described above  
166 for the EBM, as implemented by Zhang et al. (submitted). Climate changes are forced  
167 by varying the longwave optical depth in the gray radiation scheme (O'Gorman & Schnei-  
168 der, 2008). The control simulation optical depth at the surface varies meridionally, ac-  
169 cording to  $\tau_e + (\tau_p - \tau_e) \sin^2 \phi$ , with  $\tau_e = 7.2$  and  $\tau_p = 3.6$ . The vertical structure of  
170 the optical depth is the same as in O'Gorman and Schneider (2008), and the perturba-  
171 tion simulations have a 50% larger optical depth. As in the perturbed EBM climates,  
172 this is a sufficient amplitude forcing for the GCM climate to enter a perennial ice-free  
173 state.

174 The GCM simulations use T42 spectral resolution ( $\approx 2.8^\circ$  horizontal resolution)  
175 with 30 vertical levels. They are integrated for 30 years with a 600 s timestep, and we  
176 present averages over the last 20 years.

177 The GCM closely follows the EBM formulation with the following differences. The  
178 insolation and prescribed planetary albedo differ somewhat, though control values of ab-  
179 sorbed solar radiation at the top-of-atmosphere are in good agreement (Fig. S1). The  
180 GCM atmosphere explicitly simulates atmosphere's large-scale turbulence, in ways that  
181 potentially depart from the constant diffusivity formulation of the EBM. The GCM at-  
182 mosphere additionally has full vertical structure, including a representation of moist con-  
183 vection. This allows for spatially varying lapse rate feedback. As a result of these dif-  
184 ferences, the GCM has a more stable temperature feedback and a weaker destabilizing  
185 ice albedo feedback than the corresponding EBM, and hence the magnitude of the global-  
186 mean radiative forcing is roughly three times that of the EBM to produce a compara-  
187 ble climate response.

### 2.3 Experiment Hierarchy

The models described above are the most comprehensive versions of the “Moist EBM” and GCM presented in this study. Further, we incrementally disable ice thermodynamics, the seasonal cycle of insolation, ice albedo, and the effect of latent energy on the EBM’s diffusive representation of atmospheric energy transport in order to assess their relative contributions to polar amplification in our idealized framework:

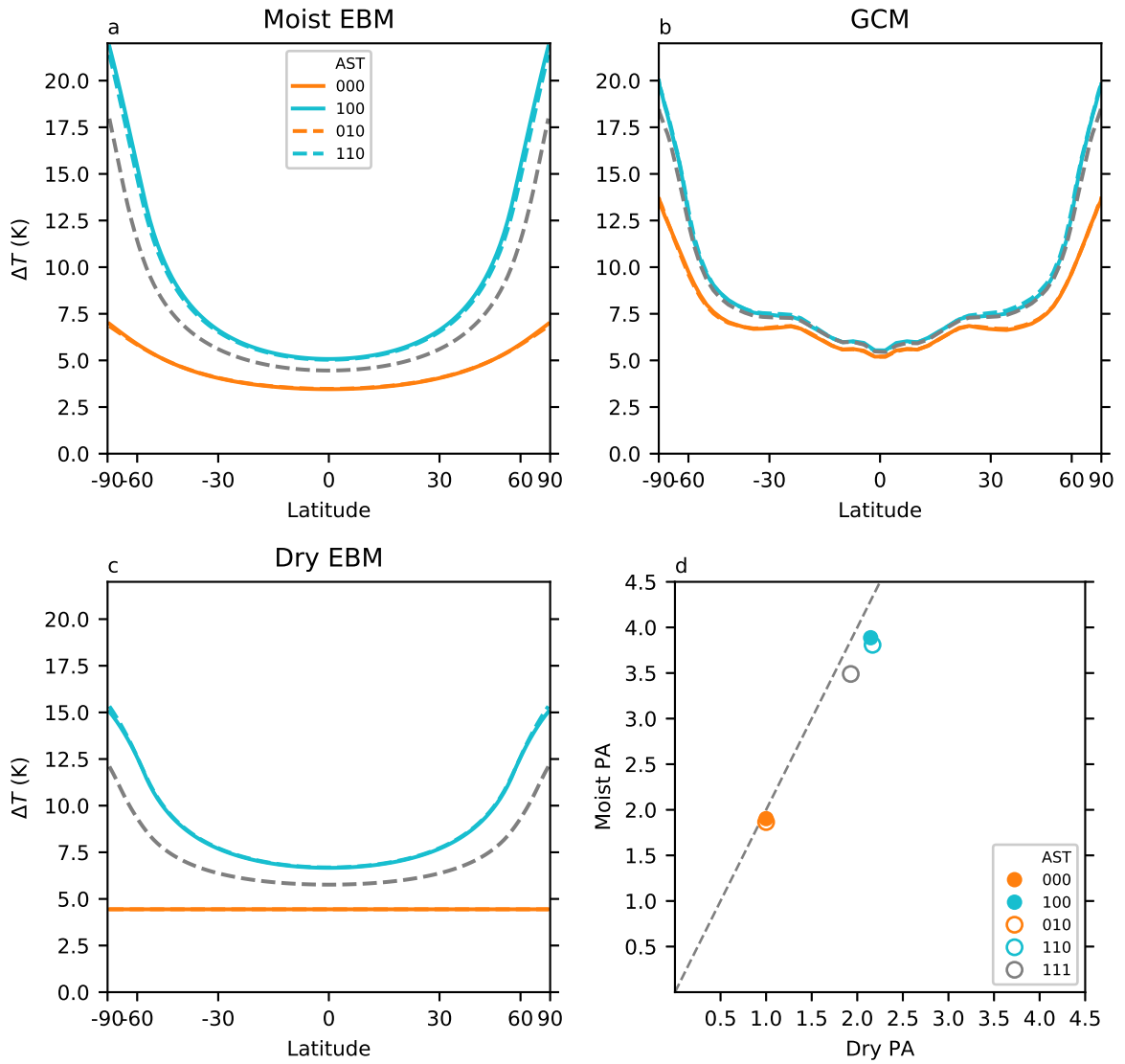
- *Ice thermodynamics* - Our most comprehensive simulations. In addition to an ice-thickness-dependent surface temperature, they also include a temperature-dependent albedo and hence an ice-albedo feedback.
- *Simple ice-albedo feedback* - Sea-ice thermodynamics are eliminated while retaining the surface-albedo temperature dependence  $\alpha(T)$  by evolving the surface enthalpy assuming a surface of 60 m of water and permitting sub-freezing temperatures. Hence, surface temperature is given everywhere by the open-water condition ( $E/c_w$ ).
- The seasonal cycle is eliminated from the EBM by setting  $S_1 = 0 \text{ W m}^{-2}$  and by using the annual-mean of the seasonal insolation for all times in the GCM.
- *Ice-free* - Ice albedo and ice thermodynamics are both eliminated by setting the albedo equal to its spatially varying open-water value.
- *“Dry EBM”* - In the case of the EBM, the effect of latent energy is eliminated by setting  $\mathcal{H} = 0$ . As is typical, the diffusivity  $D$  is doubled to  $0.6 \text{ W m}^{-2} \text{ K}^{-1}$  to maintain an Earth-like atmospheric energy transport (Flannery, 1984). The Dry EBM is identical to that of Wagner and Eisenman (2015), aside from certain parameter values and a global, rather than single-hemisphere, domain.

For the Dry EBM, we use a control radiative forcing of  $\mathcal{F} = 2 \text{ W m}^{-2}$  to represent a comparable mean-state to the Moist EBM, and it is increased to  $\mathcal{F} = 10 \text{ W m}^{-2}$  in the perturbation simulation. Ice thermodynamics, the seasonal cycle of insolation, and ice albedo can be additionally eliminated from the Dry EBM.

## 3 Results

The climate response to a radiative forcing in the Moist EBM and GCM organize into three groupings (Figure 1a,b). Climate change with a simple ice-albedo feedback, either with or without seasons, exhibits the greatest polar amplification. The addition of ice thermodynamics with seasons reduces warming at all latitudes and reduces polar amplification, particularly in the EBM. When ice thermodynamics without seasons is included, on the other hand, the response is identical (GCM) and nearly identical (EBM) to the climate response with a simple ice-albedo feedback (not shown), and in what follows we limit the thermodynamic-ice simulations to the seasonal case only. The amount of polar amplification for these icy regimes is comparable between the EBM and GCM, with a polar amplification factor of 3-4.

Climate change in the absence of ice, either with or without seasons, is characterized by less polar amplification than in the presence of ice feedbacks (orange lines in Fig. 1a,b). The result that polar amplification is merely reduced rather than eliminated is consistent with prior studies with moist EBMs (Roe et al., 2015; Merlis & Henry, 2018; Armour et al., 2019). However, that reduction is substantially less in the GCM, which overall exhibits less range in climate responses. Because the change in net solar radiation is zero in the ice-free EBM and GCM, the different responses must ultimately derive from differences in the model representations of atmospheric energy transport (i.e., diffusive in the EBM versus macroturbulent in the GCM) or the presence of a lapse rate feedback in the GCM. Notably, the inclusion of seasons in these idealized simulations has no effect on the magnitude and structure of annual-mean warming.



**Figure 1.** Polar amplification in the Moist EBM, GCM, and Dry EBM. (a) Annual-mean temperature response to an  $8 \text{ W m}^{-2}$  radiative forcing in the Moist EBM. (b) Annual-mean zonal-mean surface air temperature response to a 50% increase in longwave optical thickness in the GCM. (c) Annual-mean temperature response to an  $8 \text{ W m}^{-2}$  radiative forcing in the Dry EBM. (d) Polar amplification in the Moist EBM compared to the Dry EBM, where the polar amplification factor (PA) is calculated as the ratio of polar (65-90N) to tropical (0-6N) warming. The grey dashed reference line has a slope of 2. Simulation codes in the legend indicate whether ice albedo (A), seasonal cycle of insolation (S), or ice thermodynamics (T) are active: 000 (ice free), 010 (ice free with seasons), 100 (simple ice-albedo feedback), 110 (simple ice-albedo feedback with seasons), 111 (ice thermodynamics with seasons).

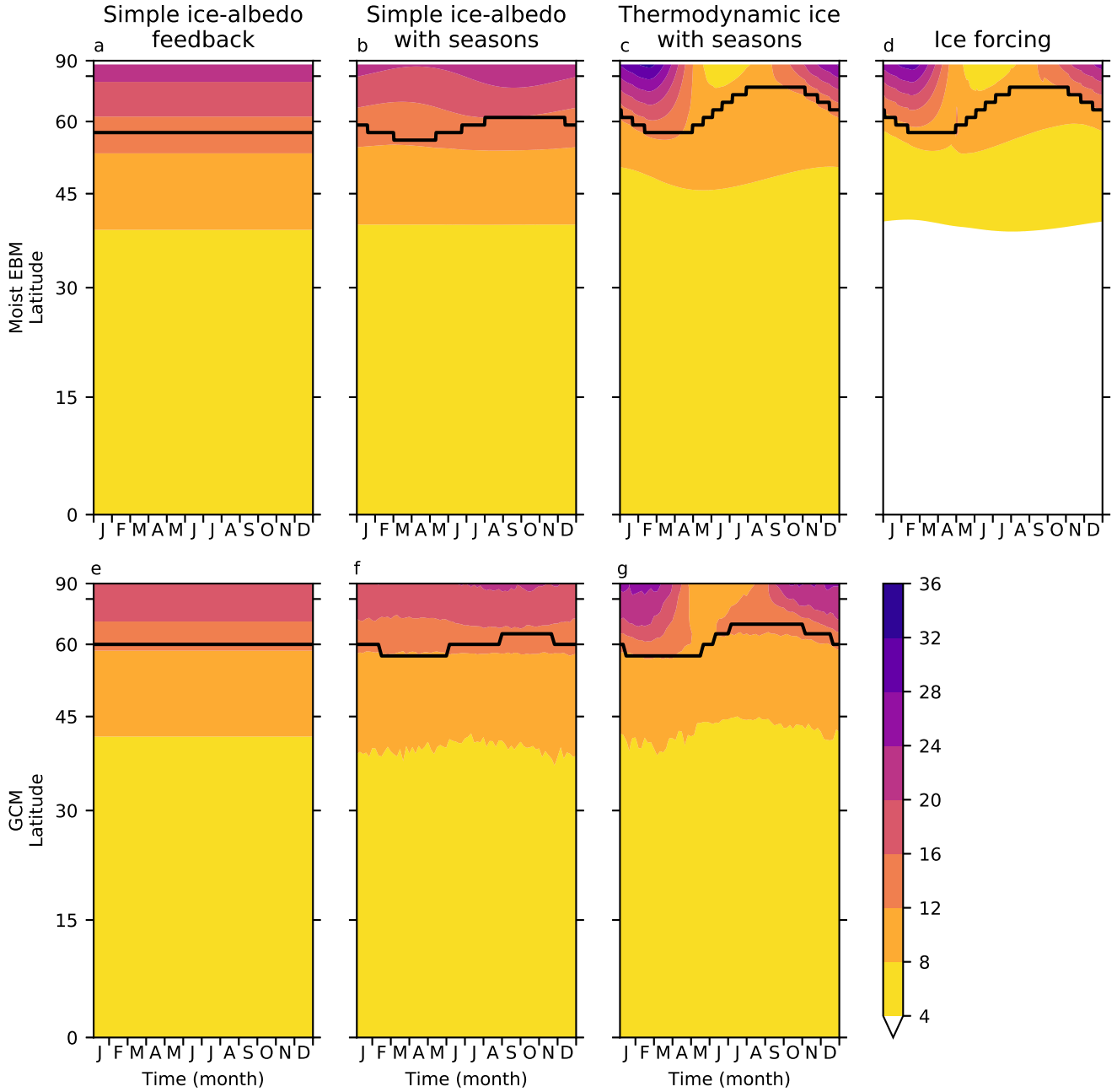
237 To understand why polar amplification is reduced in the Moist EBM with ice ther-  
 238 modynamics, we compare the seasonal cycle of temperature change across the sub-hierarchy  
 239 of icy simulations (Fig. 2, top). The reduced amplification is clearly revealed to be a sum-  
 240 mer phenomenon (Fig. 2b,c). Examination of the climatological position of the ice line  
 241 shows that thermodynamic ice has greater seasonal variability: the seasonal sea-ice max-  
 242 imum extends to the same latitude as for a simple ice-albedo feedback, however, the sea-  
 243 sonal sea-ice minimum exhibits climatologically less ice. Hence, when subjected to a ra-  
 244 diative forcing, there is less ice retreat, a smaller increase in net solar radiation (Fig. 3a),  
 245 and less polar warming in the warm season. In contrast, during the cold season, polar  
 246 amplification is enhanced by thermodynamic-ice processes. This disparate response is  
 247 due not to a greater increase in net solar radiation (they are the same; Fig. 3a), nor to  
 248 a weaker decrease in polar MSE flux convergence (Fig. 3c). Rather, the presence of ice  
 249 thermodynamics results in a much colder base climate state (Fig. 3e), necessitating a  
 250 larger temperature change when that ice melts. When the ice loss is prescribed as a forc-  
 251 ing (Fig. 2d), the resulting melting explains essentially all of the summer polar warm-  
 252 ing and is approximately 4 K less than the total response to a radiative forcing (cf. Fig.  
 253 2c).

254 These two characteristics of thermodynamic ice—small ice extent during the warm  
 255 season and thick, cold ice during the cold season—are both a consequence of the non-  
 256 linear growth rate of ice (4). Thin ice grows *and* melts faster than thick ice. However,  
 257 the melt case is limited because once  $T_0$  warms to the melting point,  $T = T_m$ . Freez-  
 258 ing ice has no such temperature constraint. Hence, the effect of ice thermodynamics is  
 259 to permit large seasonal excursions in ice extent characterized by summer temperatures  
 260 near the melting point, by thin warm-season ice, and by thick cold-season ice with sur-  
 261 face temperatures substantially below the freezing point. As noted by Eisenman and Wet-  
 262 tlauffer (2009), the nonlinearity also allows stable seasonally ice-free climate states. In-  
 263 deed, in simulations with more modest climate changes where ice persists in the cold sea-  
 264 son (not shown), the same mechanism determining the seasonal cycle of temperature change  
 265 applies because the difference between the surface air and freezing temperature decreases  
 266 with the ice thickness (4). The small-forcing warming pattern is thus also characterized  
 267 by minimal summer warming and, when cold-season ice thins and partially retreats, en-  
 268 hanced warming.

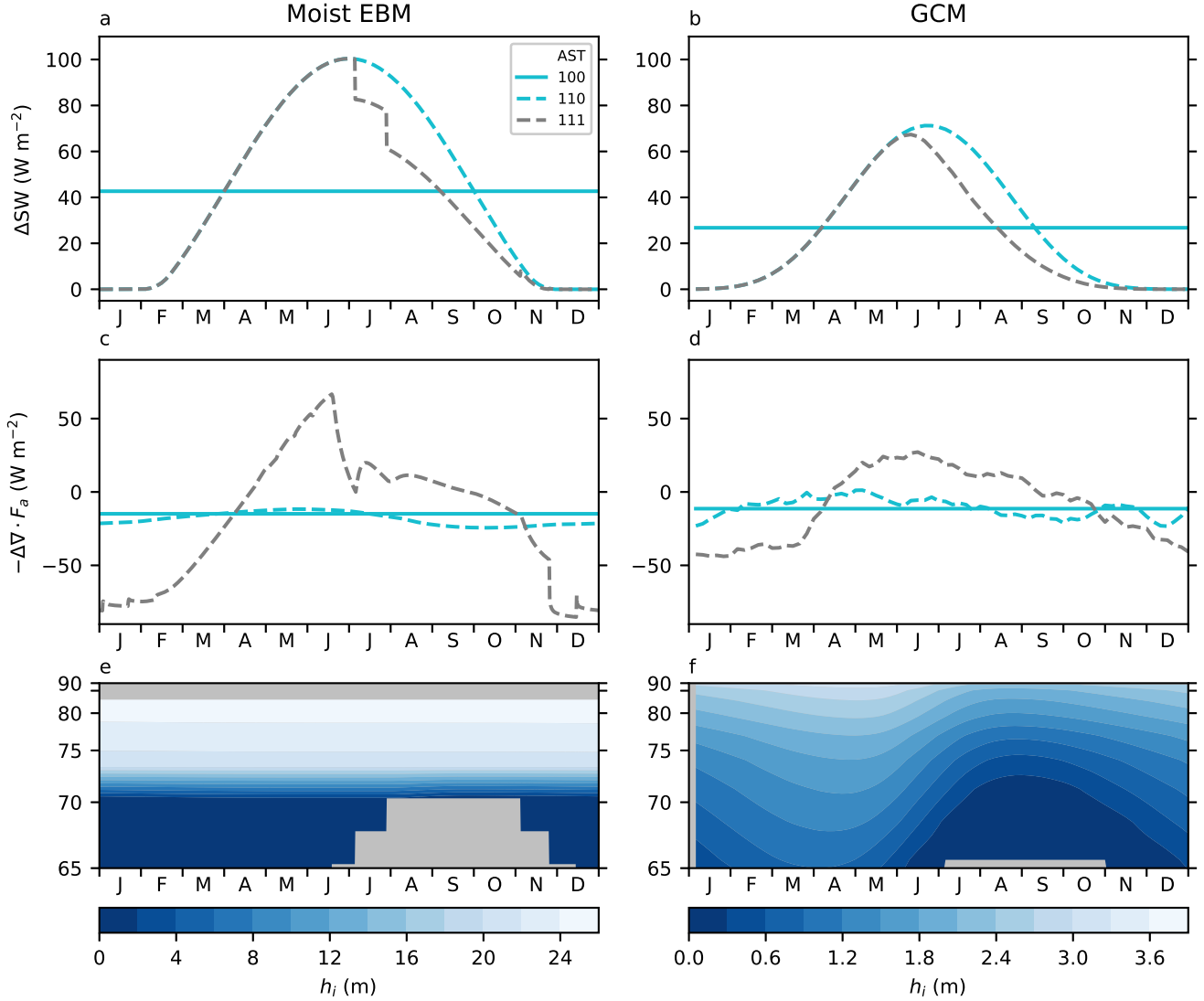
269 The seasonal cycle of polar amplification is expressed differently with a simple ice-  
 270 albedo feedback. Polar warming reaches its maximum in the warm season and its min-  
 271 imum in the cold season (Fig. 2b). A warm-season polar warming maximum can be ex-  
 272 plained by substantial ice retreat and, as a consequence, a large increase in net solar ra-  
 273 diation (Fig. 3a). Additionally, the increase in absorbed solar radiation goes directly to  
 274 raising temperatures rather than to melting ice. However, in neglecting the thermodynamic-  
 275 ice processes described above, the seasonality of warming becomes inconsistent with com-  
 276 prehensive simulations and observations of polar warming. Hence, caution should be ex-  
 277 ercised when applying the moist, seasonal EBM with a simple ice-albedo feedback be-  
 278 yond the annual-mean climate response.

279 The seasonal cycle of temperature change in the GCM sub-hierarchy (Fig. 2, bot-  
 280 tom) is broadly consistent with the Moist EBM. For a simple ice-albedo feedback, the  
 281 seasonal cycle of ice extent is muted (Fig. 2f), and extensive ice retreat occurs in all sea-  
 282 sons. Polar warming is greatest in the warm season, attendant with a relatively large in-  
 283 crease in TOA net SW radiation (Fig. 3b) that is less than the EBM change in net so-  
 284 lar radiation due to a smaller contrast in coalbedo of ocean and ice. Including thermodynamic-  
 285 ice processes makes conditions less favorable for the maintenance of warm-season ice in  
 286 the mean state. Hence, the increase in TOA net SW radiation (Fig. 3b) and polar warm-  
 287 ing (Fig. 2g) are relatively weak in the warm season, and it is the loss of thick cold-season  
 288 ice (Fig. 3f) that produces substantial polar warming. In contrast to the Moist EBM,  
 289 the summer polar warming in the GCM is not as strongly reduced by the presence of





**Figure 2.** Seasonal cycle of temperature change in the Moist EBM and GCM in the presence of (a,e) a simple ice-albedo feedback (annual-mean insolation), (b,f) a simple ice-albedo feedback, and (c,g) ice thermodynamics. The black contour is the position of the climatological ice line (0% sea-ice concentration contour). As in Fig. 1, the GCM’s surface air temperature is shown. (d) Seasonal cycle of temperature change for prescribed ice loss and constant radiative forcing ( $\mathcal{F} = 8 \text{ W m}^{-2}$ ). The temperature response to ice forcing is calculated as the difference between a Moist EBM simulation with freely evolving thermodynamic ice and a simulation with ice locked to its mean-state location and thickness.



**Figure 3.** Change in polar energy flux diagnostics and climatological ice thickness for the Moist EBM and GCM. (a,b) Change in TOA net shortwave radiation (65-90N) in the presence of a simple ice-albedo feedback (100; annual-mean insolation), a simple ice-albedo feedback (110), and ice thermodynamics (111). (c,d) Change in convergence of MSE flux (65-90N) for the same simulations as in (a,b), with a one-month running mean applied to the GCM polar-average change in MSE flux convergence. (e,f) Ice thickness in simulations with ice thermodynamics.

ice thermodynamics, and, accordingly, the annual-mean temperature changes are less sensitive to different representations of ice processes (Fig. 1). Additionally, summertime exhibits a substantial increase in convergence of MSE flux into polar regions that is essentially absent for a simple ice-albedo feedback (Fig. 3d). The seasonal transition from anomalous convergence to anomalous divergence is consistent with the much greater weakening of MSE gradients under strong cold-season polar amplification.

We disable latent heat transport to elucidate the extent to which moist atmospheric processes and sea-ice processes interact to determine annual-mean polar amplification. In the Dry EBM, polar amplification is reduced across the hierarchy (Fig. 1c). The poles systematically warm less, and the tropics warm more. The previously identified groupings remain: climate change with a simple ice-albedo feedback exhibits greatest polar amplification, climate change with ice thermodynamics exhibits moderate polar amplification, and climate change in the absence of ice produces no polar amplification. As before, the presence of seasons has no effect on the magnitude and structure of warming. Notably, polar amplification in the Dry EBM is approximately half that of the Moist EBM. If the ice-albedo feedback and latent heat transport were perfectly additive in their contributions to polar amplification, then we would expect each to produce, for instance, a doubling and their combined contribution to produce a quadrupling; in other words, we would expect the amplification factors in Figure 1c to fall along the 2:1 line. Starting from the ice-free Dry EBM ( $PA = 1$ ), adding latent heat transport has a slightly smaller influence ( $PA = 1.90$ ) than adding a simple ice-albedo feedback ( $PA = 2.15$ ), and their combined influence ( $PA = 3.89$ ) is slightly less than their sum for the Moist EBM without seasons. A linear least-squares regression yields a slope of 1.7 across the range of representations of ice processes (not shown).

## 4 Conclusions

In this study, we have exploited a gap in climate model simulations to elucidate the role of, and interactions between, ice processes, the seasonal cycle, and moist processes in determining the polar-amplified pattern of warming. Further, we systematically compare the representation of the atmospheric flow: an idealized global circulation model resolves the atmospheric macroturbulence, while a diffusive energy balance model represents the net effect of this large-scale turbulence as a down-gradient, diffusive process. These simulations reveal that the inclusion of an ice-albedo feedback via a simple temperature-dependent surface albedo promotes polar amplification in the annual mean, as expected, however, the seasonal cycle of the temperature response exhibits a warm-season maximum that is inconsistent with comprehensive climate model projections. Adding complexity to the sea-ice processes in the form of a vertical heat flux upward through the ice modestly offsets the annual-mean polar-amplified warming and profoundly affects the seasonal cycle of polar-amplified warming. In these thermodynamic-ice simulations, enhanced winter warming occurs in both the EBM and GCM, a finding previously identified by Held (1982).

The seasonal cycle of insolation has essentially no effect on annual-mean polar amplification (in contrast to comprehensive models that include cloud radiative feedbacks, e.g., Kim et al., 2018) and little effect on the seasonality of polar-amplified warming—until sea-ice thermodynamic processes are included. Here, the seasonal polar warming arises as a consequence of the climatological ice state, which is characterized by large seasonal excursions in ice extent. Thin ice thins seasonally in summer while constrained to the melting point, and thin ice thickens in winter, promoting very cold surface temperatures (Eisenman & Wettlaufer, 2009). Hence, under radiatively forced warming, the melting of thick ice produces a much larger temperature response than the melting of thin ice. The seasonality of polar-amplified warming may equivalently be understood in terms of the different heat capacities of ice and water: ice loss enhances the sensitivity of wintertime temperature by eliminating the temperature difference between atmosphere and

342 ocean, i.e., by increasing the effective surface heat capacity. Hence the climate transi-  
343 tion from thick ice to water, as illustrated in the EBM, is characterized by more energy  
344 that goes into melting summertime ice than raising temperatures, large wintertime heat  
345 capacity changes, and large seasonal variations in the temperature response. The smaller  
346 seasonal warming variability in the GCM is consistent with a transition from relatively  
347 thin ice to water, though we note that differences in radiative forcing may also contribute.

348 The role of moist energy transport is critical in giving rise to polar-amplified warm-  
349 ing in the absence of ice feedbacks, consistent with prior studies (Roe et al., 2015; Merlis  
350 & Henry, 2018; Armour et al., 2019). Furthermore, the Moist EBM simulations have a  
351 factor of 1.7 greater polar amplification across the range of representations of ice pro-  
352 cesses relative to corresponding Dry EBM simulations. This is suggestive of a superpo-  
353 sition: in isolation, ice processes amplify polar warming; in isolation, moist processes am-  
354 plify polar warming; together, ice and moist processes lead to amplified polar warming  
355 that is comparable to the sum of the individual roles. Additionally, while the represen-  
356 tation of atmospheric flow quantitatively influences the annual-mean polar amplification,  
357 qualitative sensitivities to different ice representations are similar in the EBM and GCM.  
358 Notably, in these simulations moist transport can directly influence polar warming, how-  
359 ever, it cannot influence warming via the water vapor feedback (e.g., Henry et al., 2021)  
360 or cloud feedbacks (Yoshimori et al., 2017; Graverson & Langen, 2019).

361 In conclusion, our systematic investigations in two idealized models provide evi-  
362 dence that all three mechanisms, ice processes, moist processes, and the seasonal cycle  
363 of insolation, are crucial for capturing the annual-mean and, importantly, seasonal pat-  
364 tern of polar-amplified warming. While the seasonal insolation cycle has no effect on the  
365 annual-mean polar amplification with a simple ice-albedo feedback, neglecting it results  
366 in a lack of fidelity of the seasonal cycle of warming with respect to projections from com-  
367 prehensive models. Furthermore, the seasonal solar forcing is fundamental in setting the  
368 climatological thermodynamic ice state that preconditions the ice-albedo feedback un-  
369 der more realistic ice representations. That feedback is weaker than that of a simple ice-  
370 albedo feedback and would contribute less to polar warming using popular TOA diag-  
371 nostic frameworks (e.g., Pithan & Mauritsen, 2014). However, the weak surface albedo  
372 feedback conceals large seasonal changes in temperature, which would tend to promote,  
373 given stable stratification of the lower troposphere, a positive wintertime lapse rate feed-  
374 back (e.g., Feldl et al., 2020). Those temperature changes also fundamentally drive the  
375 seasonal changes in polar energy flux convergence and reflect the seasonal changes in sur-  
376 face heat storage. The importance of such processes in interactively determining the feed-  
377 back justifies our approach of using a climatological energy balance model. While ques-  
378 tions remain regarding cloud interactions, our findings of comparable and nearly addi-  
379 tive contributions of the ice-albedo feedback and moist transport provide a basis for re-  
380 fined assessment of attributions of Arctic amplification.

## 381 Acknowledgments

382 We are grateful to Till Wagner, Ian Eisenman, and Xiyue (Sally) Zhang for providing  
383 EBM and GCM codes that enabled this research. Support was provided by National Sci-  
384 ence Foundation award AGS-1753034 (NF) and a Compute Canada/Canada Founda-  
385 tion for Innovation computing allocation and a Canada Research Chair (TMM). Datasets  
386 for this research are available at <http://doi.org/10.5281/zenodo.4738006>.

## 387 References

- 388 Alexeev, V. A., Langen, P. L., & Bates, J. R. (2005). Polar amplification of sur-  
389 face warming on an aquaplanet in "ghost forcing" experiments without sea ice  
390 feedbacks. *Climate Dynamics*, *24*, 655–666. doi: 10.1007/s00382-005-0018-3  
391 Armour, K. C., Siler, N., Donohoe, A., & Roe, G. H. (2019). Meridional atmospheric

- 392 heat transport constrained by energetics and mediated by large-scale diffusion.  
 393 *Journal of Climate*, *32*(12), 3655–3680. doi: 10.1175/JCLI-D-18-0563.1
- 394 Bitz, C. M., & Roe, G. H. (2004). A mechanism for the high rate of sea ice thinning  
 395 in the Arctic Ocean. *Journal of Climate*, *17*(18), 3623–3632. doi: 10.1175/1520  
 396 -0442(2004)017<3623:AMFTHR>2.0.CO;2
- 397 Boeke, R. C., & Taylor, P. C. (2018). Seasonal energy exchange in sea ice retreat re-  
 398 gions contributes to differences in projected Arctic warming. *Nature Communi-  
 399 cations*, *9*. doi: 10.1038/s41467-018-07061-9
- 400 Bonan, D. B., Armour, K. C., Roe, G. H., Siler, N., & Feldl, N. (2018). Sources of  
 401 uncertainty in the meridional pattern of climate change. *Geophysical Research  
 402 Letters*, *45*, 9131–9140. doi: 10.1029/2018GL079429
- 403 Budyko, M. I. (1969). The effect of solar radiation variations on the climate of the  
 404 Earth. *Tellus*, *21*, 611–619. doi: 10.3402/tellusa.v21i5.10109
- 405 Dai, A., Luo, D., Song, M., & Liu, J. (2019). Arctic amplification is caused by sea-  
 406 ice loss under increasing CO<sub>2</sub>. *Nature Communications*, *10*, 121. doi: 10.1038/  
 407 s41467-018-07954-9
- 408 Eisenman, I., & Wettlaufer, J. S. (2009). Nonlinear threshold behavior during the  
 409 loss of Arctic sea ice. *Proceedings of the National Academy of Sciences of the  
 410 United States of America*, *106*(1), 28–32. doi: 10.1073/pnas.0806887106
- 411 Feldl, N., Bordoni, S., & Merlis, T. M. (2017). Coupled high-latitude climate feed-  
 412 backs and their impact on atmospheric heat transport. *Journal of Climate*,  
 413 *30*(1), 189–201. doi: 10.1175/JCLI-D-16-0324.1
- 414 Feldl, N., Po-Chedley, S., Singh, H. K., Hay, S., & Kushner, P. J. (2020). Sea ice  
 415 and atmospheric circulation shape the high-latitude lapse rate feedback. *npj  
 416 Climate and Atmospheric Science*, *3*. doi: 10.1038/s41612-020-00146-7
- 417 Flannery, B. P. (1984). Energy balance models incorporating transport of thermal  
 418 and latent energy. *Journal of the Atmospheric Sciences*, *41*(3), 414–421. doi:  
 419 10.1175/1520-0469(1984)041<0414:EBMITO>2.0.CO;2
- 420 Frierson, D. M. W., Held, I. M., & Zurita-Gotor, P. (2006). A gray-radiation aqua-  
 421 planet moist GCM. Part I: Static stability and eddy scale. *Journal of the At-  
 422 mospheric Sciences*, *63*(10), 2548–2566. doi: 10.1175/JAS3753.1
- 423 Frierson, D. M. W., Held, I. M., & Zurita-Gotor, P. (2007). A gray-radiation aqua-  
 424 planet moist GCM. Part II: Energy transports in altered climates. *Journal of  
 425 the Atmospheric Sciences*, *64*(5), 1680–1693. doi: 10.1175/JAS3913.1
- 426 Graverson, R. G., & Langen, P. L. (2019). On the role of the atmospheric energy  
 427 transport in 2CO<sub>2</sub>-induced polar amplification in CESM1. *Journal of Climate*,  
 428 *32*(13), 3941–3956. doi: 10.1175/JCLI-D-18-0546.1
- 429 Held, I. M. (1982). Climate models and the astronomical theory of the ice ages.  
 430 *Icarus*, *50*(2-3), 449–461. doi: 10.1016/0019-1035(82)90135-X
- 431 Henry, M., Merlis, T. M., Lutsko, N. J., & Rose, B. E. (2021). Decomposing the  
 432 Drivers of Polar Amplification with a Single Column Model. *Journal of Cli-  
 433 mate*, *34*(6), 2355–2365. doi: 10.1175/jcli-d-20-0178.1
- 434 Holland, M. M., & Bitz, C. M. (2003). Polar amplification of climate change in cou-  
 435 pled models. *Climate Dynamics*, *21*, 221–232. doi: 10.1007/s00382-003-0332  
 436 -6
- 437 Hwang, Y.-T., & Frierson, D. M. W. (2010). Increasing atmospheric poleward en-  
 438 ergy transport with global warming. *Geophysical Research Letters*, *37*(24). doi:  
 439 10.1029/2010GL045440
- 440 Hwang, Y.-T., Frierson, D. M. W., & Kay, J. E. (2011). Coupling between Arct-  
 441 ic feedbacks and changes in poleward energy transport. *Geophysical Research  
 442 Letters*, *38*(17). doi: 10.1029/2011GL048546
- 443 Kim, D., Kang, S. M., Shin, Y., & Feldl, N. (2018). Sensitivity of polar amplification  
 444 to varying insolation conditions. *Journal of Climate*, *31*(12), 4933–4947. doi:  
 445 10.1175/JCLI-D-17-0627.1
- 446 Langen, P. L., Graverson, R. G., & Mauritsen, T. (2012). Separation of contribu-

- 447 tions from radiative feedbacks to polar amplification on an aquaplanet. *Journal*  
448 *of Climate*, 25(8), 3010–3024. doi: 10.1175/JCLI-D-11-00246.1
- 449 Lutsko, N. J., Seeley, J. T., & Keith, D. W. (2020). Estimating impacts and trade-  
450 offs in solar geoengineering scenarios with a moist energy balance model. *Geo-*  
451 *physical Research Letters*, 47, e2020GL087290. doi: 10.1029/2020GL087290
- 452 Manabe, S., & Wetherald, R. T. (1975). The effects of doubling the CO<sub>2</sub> concentra-  
453 tion on the climate of a general circulation model. *Journal of the Atmospheric*  
454 *Sciences*, 32(1), 3–15.
- 455 Merlis, T. M. (2014). Interacting components of the top-of-atmosphere energy bal-  
456 ance affect changes in regional surface temperature. *Geophysical Research Let-*  
457 *ters*, 41, 7291–7297. doi: 10.1002/2014GL061700
- 458 Merlis, T. M., & Henry, M. (2018). Simple estimates of polar amplification in moist  
459 diffusive energy balance models. *Journal of Climate*, 31(15), 5811–5824. doi:  
460 10.1175/JCLI-D-17-0578.1
- 461 North, G. R. (1975). Theory of energy-balance climate models. *Journal of the Atmo-*  
462 *spheric Sciences*, 32(11), 2033–2043. doi: 10.1175/1520-0469(1975)032<2033:  
463 TOEBCM>2.0.CO;2
- 464 North, G. R., Cahalan, R. F., & Coakley, J. A. (1981). Energy balance climate mod-  
465 els. *Reviews of Geophysics*, 19(1), 91. doi: 10.1029/RG019i001p00091
- 466 O’Gorman, P. A., & Schneider, T. (2008). The hydrological cycle over a wide range  
467 of climates simulated with an idealized GCM. *Journal of Climate*, 21(15),  
468 3815–3832. doi: 10.1175/2007JCLI2065.1
- 469 Pithan, F., & Mauritsen, T. (2014). Arctic amplification dominated by temperature  
470 feedbacks in contemporary climate models. *Nature Geoscience*, 7(3), 181–184.  
471 doi: 10.1038/ngeo2071
- 472 Roe, G. H., Feldl, N., Armour, K. C., Hwang, Y.-T., & Frierson, D. M. W. (2015).  
473 The remote impacts of climate feedbacks on regional climate predictability.  
474 *Nature Geoscience*, 8(2), 135–139. doi: 10.1038/ngeo2346
- 475 Rose, B. E. J., Armour, K. C., Battisti, D. S., Feldl, N., & Koll, D. D. B. (2014).  
476 The dependence of transient climate sensitivity and radiative feedbacks on the  
477 spatial pattern of ocean heat uptake. *Geophysical Research Letters*, 41. doi:  
478 10.1002/2013GL058955
- 479 Russotto, R. D., & Biasutti, M. (2020). Polar amplification as an inherent re-  
480 sponse of a circulating atmosphere: Results from the TRACMIP aqua-  
481 planets. *Geophysical Research Letters*, 47(6), e2019GL086771. doi:  
482 10.1029/2019GL086771
- 483 Sellers, W. D. (1969). A global climatic model based on the energy balance of the  
484 Earth-atmosphere system. *Journal of Applied Meteorology*, 8(3), 392–400. doi:  
485 10.1175/1520-0450(1969)008<0392:agcmbo>2.0.co;2
- 486 Wagner, T. J. W., & Eisenman, I. (2015). How climate model complexity influences  
487 sea ice stability. *Journal of Climate*, 28(10), 3998–4014. doi: 10.1175/jcli-d-14-  
488 -00654.1
- 489 Winton, M. (2006). Amplified Arctic climate change: What does surface albedo  
490 feedback have to do with it? *Geophysical Research Letters*, 33(3). doi: 10  
491 .1029/2005GL025244
- 492 Yoshimori, M., Abe-Ouchi, A., & L ain e, A. (2017). The role of atmospheric heat  
493 transport and regional feedbacks in the Arctic warming at equilibrium. *Cli-*  
494 *mate Dynamics*, 49(9-10), 3457–3472. doi: 10.1007/s00382-017-3523-2
- 495 Zhang, X., Schneider, T., Shen, Z., Pressel, K., & Eisenman, I. (submitted). Sea-  
496 sonal cycle of idealized polar clouds: Large eddy simulations driven by a GCM.  
497 *Journal of Advances in Modeling Earth Systems*.